| 1 | (i) | State $\mathrm{f}(x) \leq 10$ | B1 | 1 [Any equiv but must be or imply $\leq$ ] |
| :---: | :---: | :---: | :---: | :---: |
|  | (ii) | Attempt correct process for composition of functions <br> Obtain 6 or correct expression for $\mathrm{ff}(x)$ <br> Obtain - 71 | M1 <br> A1 <br> A1 | [whether algebraic or numerical] |
| 2 |  | Either Obtain $x=0$ <br> Form linear equation with signs of $6 x$ and $x$ different <br> State $6 x-1=-x+1$ <br> Obtain $\frac{2}{7}$ and no other non-zero value | B1 <br> M1 <br> A1 <br> A1 | [ignoring errors in working] [ignoring other sign errors] <br> [or correct equiv with or without brackets] <br> 4 [or exact equiv] |
|  | Or | Obtain $36 x^{2}-12 x+1=x^{2}-2 x+1$ <br> Attempt to solve quadratic equation <br> Obtain $\frac{2}{7}$ and no other non-zero value Obtain 0 | B1 <br> M1 <br> A1 <br> B1 | [or equiv] <br> [as far as factorisation or subn into formula] <br> [or exact equiv] <br> (4) [ignoring errors in working] |
| 3 | (i) | Attempt solution involving (natural) logarithm <br> Obtain $-0.017 t=\ln \frac{25}{180}$ <br> Obtain 116 | M1 <br> A1 <br> A1 | [or equiv] <br> 3 [or greater accuracy rounding to 116] |
|  | (ii) | Differentiate to obtain $k \mathrm{e}^{-0.017 t}$ <br> Obtain correct $-3.06 \mathrm{e}^{-0.017 t}$ <br> Obtain 1.2 | M1 <br> A1 <br> A1 | [any constant $k$ different from 180; solution must involve differentiation] <br> [or unsimplified equiv; accept + or -] <br> 3 [or greater accuracy; accept + or - answer] |
| 4 | (a) | State or imply $\int \pi y^{2} \mathrm{~d} x$ Integrate to obtain $k \ln x$ <br> Obtain $4 \pi \ln x$ or $4 \ln x$ Obtain $4 \pi \ln 5$ | B1 <br> M1 <br> A1 <br> A1 | [any constant $k$, involving $\pi$ or not; or equiv such as $k \ln 4 x$ ] [or equiv] <br> 4 [or similarly simplified equiv] |


|  | (b) | Attempt calculation involving attempts at $y$ values <br> Attempt $\frac{1}{3} \times 1\left(y_{0}+4 y_{1}+2 y_{2}+4 y_{3}+y_{4}\right)$ <br> Obtain $\frac{1}{3}(\sqrt{2}+4 \sqrt{5}+2 \sqrt{10}+4 \sqrt{17}+\sqrt{26})$ <br> Obtain 12.758 | M1 <br> M1 <br> A1 <br> A1 | [with each of $1,4,2$ present at least once as coefficients] [with attempts at five $y$ values] <br> [or exact equiv or decimal equivs] <br> 4 [or greater accuracy] |
| :---: | :---: | :---: | :---: | :---: |
| 5 | (i) | Obtain $R=\sqrt{13}$, or 3.6 or 3.61 or greater accuracy <br> Attempt recognisable process for finding $\alpha$ Obtain $\alpha=33.7$ | B1 <br> M1 <br> A1 | [allow sine/cosine muddles] <br> 3 [or greater accuracy] |
|  | (ii) | Attempt to find at least one value of $\theta+\alpha$ Obtain value rounding to 76 or 104 Subtract their $\alpha$ from at least one value Obtain one value rounding to 42 or 43 , or to 70 <br> Obtain other value 42.4 or 70.2 | *M1 <br> A1 $\sqrt{ }$ <br> M1 <br> A1 <br> A1 | [following their $R$ ] <br> [dependent on *M] <br> 5 [or greater accuracy; no other answers between 0 and 360 ; ignore answers outside 0 to 360] |
| 6 | (a) | Attempt use of product rule <br> Obtain $\ln x+1$ <br> Equate attempt at first derivative to zero and obtain value involving e <br> Obtain $\mathrm{e}^{-1}$ | *M1 <br> A1 <br> M1 <br> A1 | [or unsimplified equiv] [dependent on ${ }^{*} \mathbf{M}$ ] <br> 4 [or exact equiv] |
|  | (b) | Attempt use of quotient rule <br> Obtain $\frac{(4 x-c) 4-4(4 x+c)}{(4 x-c)^{2}}$ <br> Show that first derivative cannot be zero | M1 <br> A1 <br> A1 | [or equiv using product rule or ...] <br> [or equiv] <br> 3 [AG; derivative must be correct] |
| 7 | (i) | State $2 \cos ^{2} x-1$ | B1 | 1 |
|  | (ii) | Attempt to express left hand side in terms of $\cos x$ <br> Identify $\frac{1}{\cos x}$ as $\sec x$ | M1 | [using expression of form $a \cos ^{2} x+b$ ] [maybe implied] |

\begin{tabular}{|c|c|c|c|c|}
\hline \& \& Confirm result \& A1 \& 3 [AG; necessary detail required] \\
\hline \& (iii) \& \begin{tabular}{l}
Use identity \(\sec ^{2} x=1+\tan ^{2} x\) \\
Attempt solution of quadratic equation in tan \(x\) \\
Obtain \(2 \tan ^{2} x+3 \tan x-9=0\) and hence \(\tan\) \(x=-3, \frac{3}{2}\) \\
Obtain at least two of 0.983, 4.12, 1.89, 5.03 \\
(or of \(0.313 \pi, 1.31 \pi, 0.602 \pi, 1.60 \pi\) ) \\
Obtain all four solutions
\end{tabular} \& B1
M1
A1
A1

A1 \& | [or equiv] |
| :--- |
| [allow answers with only 2 s.f.; allow greater accuracy; allow $0.983+\pi, 1.89+\pi$ allow degrees: 56, 236, 108, 288] 5 [now with at least 3 s.f.; must be radians; no other solutions in the range 0-2 $\pi$, ignore solutions outside range $0-2 \pi$ ] | \\

\hline \multirow[t]{3}{*}{8} \& (i) \& | Attempt relevant calculations with 5.2 and 5.3 |
| :--- |
| Obtain correct values |
| Conclude appropriately | \& M1

A1

A1 \& | $\begin{array}{lccc} x & y_{1} & y_{2} & y_{1}-y_{2} \\ 5.2 & 2.83 & 2.87 & -0.04 \\ 5.3 & 2.89 & 2.88 & 0.006 \end{array}$ |
| :--- |
| 3 [AG; comparing $y$ values or noting sign change in difference in $y$ values or equiv] | \\

\hline \& (ii) \& | Equate expressions and attempt rearrangement to $x=$ |
| :--- |
| Obtain $x=\frac{5}{3} \ln (3 x+8)$ | \& M1

A1 \& 2 [AG; necessary detail required] \\

\hline \& (iii) \& | Obtain correct first iterate |
| :--- |
| Carry out correct process to find at least two iterates in all |
| Obtain 5.29 | \& | B1 |
| :--- |
| M1 |
| A1 | \& 3 [must be exactly 2 decimal places;

$$
\begin{aligned}
& 5.2 \rightarrow 5.2687 \rightarrow 5.2832 \rightarrow 5.2863 \rightarrow 5.2869 ; \\
& 5.25 \rightarrow 5.2793 \rightarrow 5.2855 \rightarrow 5.2868 \rightarrow 5.2870 ; \\
& 5.3 \rightarrow 5.2898 \rightarrow 5.2877 \rightarrow 5.2872 \rightarrow 5.2871]
\end{aligned}
$$ \\

\hline \& (iv) \& Obtain integral of form $k(3 x+8)^{\frac{4}{3}}$ Obtain integral of form $k \mathrm{e}^{\frac{1}{5} x}$ \& M1
M1 \& \\
\hline
\end{tabular}

|  |  | Obtain $\frac{1}{4}(3 x+8)^{\frac{4}{3}}-5 \mathrm{e}^{\frac{1}{5} x}$ <br> Apply limits 0 and their answer to (iii) <br> Obtain 3.78 | A1 <br> M1 <br> A1 | [or equiv] <br> [applied to difference of two integrals] <br> 5 [or greater accuracy] |
| :---: | :---: | :---: | :---: | :---: |
| 9 | (i) | Indicate stretch and (at least one) translation <br> State translation by 7 units in negative $x$ direction <br> State stretch in $x$ direction with factor $1 / m$ <br> Indicate translation by 4 units in negative $y$ direction | M1 <br> A1 <br> A1 <br> B1 | [... in general terms] <br> [or equiv; using correct terminology] <br> [must follow the translation by 7; or equiv; using correct terminology] <br> 4 [or equiv; at any stage; the two translations may be combined] |
|  | (ii) | Refer to each $y$ value being image of unique $x$ value <br> Attempt correct process for finding inverse <br> Obtain expression involving $(x+4)^{2}$ or $(y+4)^{2}$ <br> Obtain $\frac{(x+4)^{2}-7}{m}$ | B1 <br> M1 <br> M1 <br> A1 | [or equiv] <br> 4 [or equiv] |
|  | (iii) | Refer to fact that curves are reflections of each other in line $y=x$ <br> Attempt arrangement of either $\mathrm{f}(x)=x$ or $\mathrm{f}^{-1}(x)=x$ <br> Apply discriminant to resulting quadratic equati on <br> Obtain $(m-2)(m-14)<0$ <br> Obtain $2<m<14$ | B1 <br> M1 <br> M1 <br> A1 <br> A1 | [or equiv] <br> [or equiv] <br> 5 |

